

THE STUDY OF ACOUSTIC MODES BACK-SCATTERING BY BOTTOM RELIEF INHOMOGENEITIES USING THE INVARIANT IMBEDDING METHOD

M.S. Kazak, P.S. Petrov, K.V. Koshel

In models of sound propagation in a shallow sea with penetrable bottom, the effect of back-scattering of acoustic waves can usually be neglected. The parabolic equation method, for instance, is based on the one-way propagation approximation. Estimations of the magnitude of a back-scattered wave, nevertheless, are almost absent in the literature. In this study, such estimates are obtained in the framework of the adiabatic normal modes theory. This approximation allows us to separate the backward scattering from mode coupling, which is another important effect observed in acoustic wave propagation over bottom relief inhomogeneities. The scattering of a single normal mode on a localized bottom relief inhomogeneity is considered, and the dependence of the amplitude of the backward-scattered wave on the size of the inhomogeneity and mode number is investigated. The numerical solution of the Riccati equation is used for obtaining the reflection coefficient. The latter equation is obtained by transforming the original boundary-value problem for the Helmholtz equation for the mode amplitude to imbedding equations. The possibilities of further generalizations and applications of modal imbedding equations in the issues of underwater sound are discussed.

Keywords: ocean acoustics; normal modes method; invariant imbedding method; back-scattering.

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About the authors

KAZAK Mikhail Sergeevich, research engineer
V.I. Il'ichev Pacific Oceanological Institute of the Far Eastern Branch of the Russian Academy of Sciences
Address: 43, Baltiyskaya Street, Vladivostok, 690041, Russia
Research interests: Ocean acoustics, partial differential equations, math modelling, parabolic equation method
E-mail: kazak.ms@poi.dvo.ru
Phone: +7(902)078-89-11
ORCID ID: 0000-0002-8141-8665

PETROV Pavel Sergeevich, PhD, head of the laboratory
V.I. Il'ichev Pacific Oceanological Institute of the Far Eastern Branch of the Russian Academy of Sciences
Address: 43, Baltiyskaya Street, Vladivostok, 690041, Russia
Research interests: Ocean acoustics, partial differential equations, math modelling, parabolic equation method
E-mail: petrov@poi.dvo.ru
Phone: +7(914)960-21-92
ORCID ID: 0000-0002-0087-6681

KOSHEL Konstantin Valentinovich, doctor of Physical and Mathematical Sciences, Chief Researcher
V.I. Il'ichev Pacific Oceanological Institute of the Far Eastern Branch of the Russian Academy of Sciences
Address: 43, Baltiyskaya Street, Vladivostok, 690041, Russia
Research interests: Geophysical hydrodynamics, vortex dynamics, radiophysics, wave theory, theory of random processes and field theory, dynamical systems theory
E-mail: kvkoshel@poi.dvo.ru
Phone: +7(924)131-25-02
ORCID ID: 0000-0002-8014-7699